# **Trees**

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## 1. Trees

Tree based methods are a major player in data-mining.

#### Good:

- flexible fitters, capture non-linearity and interactions.
- do not have to think about scale of x variables.
- ▶ handles categorical and numeric y and x very nicely.
- ► fast.
- interpretable (when small).

#### Bad:

Not the best in out-of-sample predictive performance (but not bad!!).

# But,

If we **bag** or **boost** trees, we can get the best off-the-shelf prediction available.

Bagging and Boosting are *ensemble methods* that combine the fit from many (hundreds, thousands) of tree models to get an overall predictor.

# 2. Regression Trees

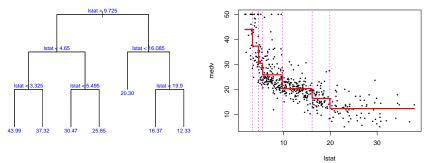
Let's look at a simple 1-dimensional example so that we can see what is going on.

We'll use the Boston housing data and relate x=lstat to y=medval.

At left is the *tree* fit to the data.

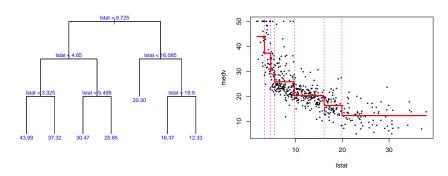
At each *interior node* there is a decision rule of the form  $\{x < c\}$ . If x < c you go left, otherwise you go right.

Each observation is sent down the tree until it hits a bottom node or *leaf* of the tree.



The set of bottom nodes gives us a partition of the predictor (x) space into disjoint regions. At right, the vertical lines display the partition. With just one x, this is just a set of intervals.

Within each region (interval) we compute the average of the y values for the subset of training data in the region. This gives us the step function which is our  $\hat{f}$ . The  $\bar{y}$  values are also printed at the bottom nodes (left plot).



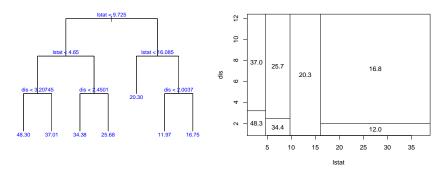
To predict, we just use our step function estimate of f(x).

Equivalently, we drop x down the tree until it lands in a leaf and then predict the average of the y values for the training observations in the same leaf.

## A Tree with Two Explanatory Variables

Here is a tree with  $x = (x_1, x_2) = (lstat, dis)$  and y = medv.

Now the decision rules can use either of the two x's.



At right is the *partition* of the x space corresponding to the set of bottom nodes (leaves).

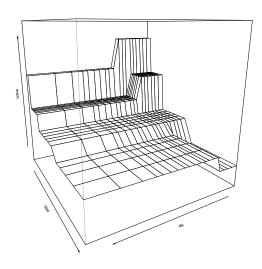
The average y for training observations assigned to a region is printed in each region and at the bottom nodes.

This is the regression function given by the tree.

It is a step function which can seem dumb, but it delivers nonlinearity *and* interactions in a simple way and works with a lot of variables.

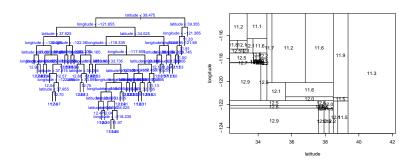
Notice the interaction.

The effect of dis depends on lstat!!



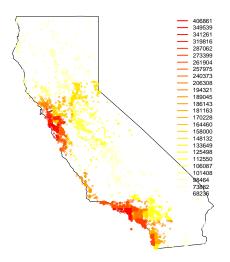
# The California Housing Data

Here is a tree with 50 bottom nodes fit to the California Housing data using only longitude and latitude.



Don't extrapolate into the ocean!

Here is a view of the fit using the map of the state. (units are dollars, the logMedVal was exponentiated for the labels).



## In R:

```
#-----
#load tree package (and MASS), attach Boston data
library(tree)
library(MASS)
#data(Boston) #don't need this
attach (Boston)
#-----
#fit a tree to boston data just using 1stat.
#first get a big tree using a small value of mindev
temp = tree(medv~lstat,data=Boston,mindev=.0001)
cat("first big tree size: \n")
print(length(unique(temp$where)))
#if the tree is too small. make mindev smaller!!
#-----
#then prune it down to one with 7 leaves
boston.tree=prune.tree(temp,best=7)
cat("pruned tree size: \n")
print(length(unique(boston.tree$where)))
```

```
#plot the tree
plot(boston.tree,type="uniform")
text(boston.tree,col="blue",label=c("yval"),cex=.8)
#-----
#plot data with fit
#get fit
boston.fit = predict(boston.tree) #get training fitted values
#plot fit
plot(lstat,medv,cex=.5,pch=16) #plot data
oo=order(lstat)
lines(lstat[oo],boston.fit[oo],col="red",lwd=3) #step function fit
#-----
#predict at 1stat = 15 and 25.
preddf = data.frame(lstat=c(15,25))
vhat = predict(boston.tree,preddf)
points(preddf$lstat,yhat,col="blue",pch="*".cex=3)
```

Let's fit the tree using 1stat and dis.

```
df2=Boston[,c(8,13,14)] #pick off dis,lstat,medv
print(names(df2))
#big tree
temp = tree(medv~.,df2,mindev=.0001)
cat("first big tree size: \n")
print(length(unique(temp$where)))
#then prune it down to one with 7 leaves
boston.tree=prune.tree(temp,best=7)
cat("pruned tree size: \n")
print(length(unique(boston.tree$where)))
# plot tree and partition in x.
par(mfrow=c(1,2))
#plot tree
plot(boston.tree.tvpe="u")
text(boston.tree,col="blue",label=c("yval"),cex=.8)
#plot 2-dimesional partition in (x1,x2) = (lstat,dis)
partition.tree(boston.tree)
```

### Lets try p = 4 with nox, rm, ptratio, and lstat.

```
df4=Boston[,c(5,6,11,13,14)] #pick off variables
print(names(df4))
temp = tree(medv~.,df4,mindev=.0001)
cat("first big tree size: \n")
print(length(unique(temp$where)))
#then prune it down to one with 15 leaves (picked 15 arbitrarily)
boston.tree4=prune.tree(temp,best=15)
cat("pruned tree size: \n")
print(length(unique(boston.tree4$where)))
#plot tree
par(mfrow=c(1,1))
plot(boston.tree4,type="u")
text(boston.tree4,col="blue",label=c("yval"),cex=.8)
#compare fits
fmat4=cbind(fmat,predict(boston.tree4))
colnames(fmat4)[4]="tree4"
pairs(fmat4)
print(cor(fmat4))
```

## 3. Classification Trees

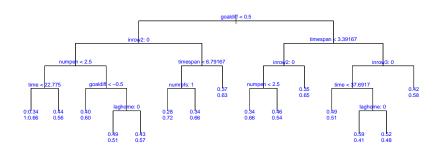
Let's do a tree for a classification problem.

We'll use the hockey penalty data.

The response is whether or not the next penalty is on the other team and x is a bunch of stuff about the game situation (the score ...).

In addition, this time some of our predictors (features, x's) are categorical.

#### Here is the tree:



- **Each** bottom node gives the fraction of training data in the two outcome categories. Think of it as  $\hat{p}$  for the kind of x associated with that bottom node.
- ► The form of the decision rule can't be x < c for categorical variables. We pick a subset of the levels to go left. inrow2:0 means all the observations with inrow2 in the category labeled 0 go left.

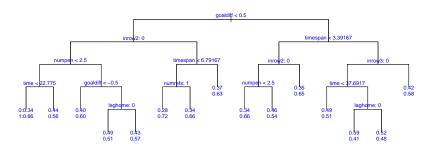
#### There is a lot of fit!!!

#### if:

- if you are not winning
- you had the last two penalties
- it has not been long since the last call
- and there is only 1 referee

#### then:

there is a 72% chance the next call will be on the other team.



Whilst there is another game situation where the chance the next call is on the other team is only 41%.

# 4. Trees: A Summary

#### Trees:

- Trees use recursive binary splits to partition the predictor space.
- Each binary split consists of a decision rule which sends x left or right.
- For numeric  $x_i$ , the decision rule is of the form if  $x_i < c$ .
- For categorical  $x_i$ , the rule lists the set of categories sent left.
- ightharpoonup The set of bottom nodes (or leaves) give a partition of the x space.
- ➤ To predict, we drop an out-of-sample x down the tree until it lands in a bottom node.
- ► For numeric *y*, we predict the average *y* value for the training data that ended up in the bottom node.
- For categorical y we use the category proportions for the training data that ended up in the bottom node.

#### Good:

- ► Handles categorical/numeric *x* and *y* nicely.
- Don't have to think about the scale of x's !!!
- Computationally fast ("scales").
- Small trees are interpretable.
- Variable selection.

#### Bad:

- Step function is crude, does not give the best predictive performance.
- Hard to assess uncertainly.
- Big trees are not interpretable.

# 5. Tree Models and the Bias Variance Trade Off

How do we fit trees to data??

The key idea is that a complex tree is simply a big tree.

We usually measure the complexity of the tree by the number of bottom nodes.

To fit a tree, we choose a tree to minimize (on the training data):

$$C(T, y) = L(T, y) + \alpha |T|$$

where,

- ▶ L(T, y) is our loss in fitting data y with tree T. We want good fit on the training data  $\Rightarrow$  want L small.
- ► |T| is the number of bottom nodes in tree T.
  But, we don't want a complex model that fits too well
  ⇒ we want |T| small.

For numeric y our loss is usually sum of squared errors, for categorical y we can use the deviance or the miss-classification rate.

$$C(T, y) = L(T, y) + \alpha |T|$$

## $\alpha$ big:

The *penalty* for having a big tree is large.

When we do our minimization, we will get a smaller tree with a bigger L on the training data.

### $\alpha$ small:

We do not mind having a big tree. We will get a smaller L (better fit) on the training data.

 $\alpha$  is analogous to k in k-NN !!!!!  $\alpha$  is analogous to  $\lambda$  in the lasso !!!!!

 $\alpha$  is called the *complexity-cost penalty parameter*.

# How do we do the minimization ??!!

Now we have a problem.

While trees are simple in some sense, once we view them as variables in an optimization they are large and complex.

A key to tree modeling is the success of the following heuristic algorithm for fitting trees to training data.

# (I. Grow Big)

Use a greedy, recursive forward search to build a big tree.

(i)

Start with the tree that is a single node.

(ii)

At each bottom node, search over all possible decision rules to find the one that gives the biggest decrease in loss (increase in fit).

(iii)

Grow a big tree, stopping (for example) when each bottom node has 5 observations in it.

### (II. Prune Back)

(i)

Recursively, prune back the big tree from step (I).

(ii)

Give a current pruned tree, examine every pair of bottom nodes (having the same parent node) and consider eliminating the pair.

Prune the pair the gives the biggest decrease in our criterion C.

This is give us a sequence of subtrees of our initial big tree.

(iii)

For a given  $\alpha$ , choose the subtree of the big tree that has the smallest C.

# So,

Give training data and  $\alpha$  we get a tree.

#### How do we choose $\alpha$ ??

As usual, we can leave out a validation data set and choose the  $\alpha$  the performs best on the validation data, or use k-fold cross validation.

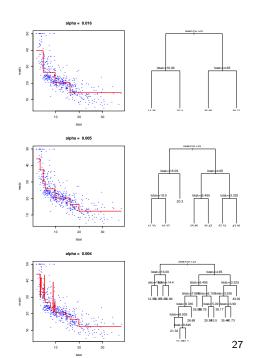
# Boston Data, Istat and medv:

At right are three different tree fits we get from three different  $\alpha$  values (using all the data).

The smaller  $\alpha$  is, the lower the penalty for complexity is, the bigger tree you get.

The top tree is a sub-tree of the middle tree, and the middle tree is a sub-tree of the bottom tree.

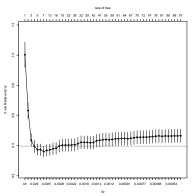
The middle  $\alpha$  is the one suggested by CV.



This is the CV plot giving by the R package rpart for y=medv x=Istat.

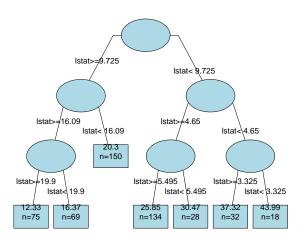
Tree sizes at top of plot, and (a transformation of)  $\alpha$  (the "cost-complexity" parameter) on the bottom.

The error is relative to the error obtained with a single node (fit is  $y = \bar{y}$ ,  $\alpha = \infty$ ).



Caution: the bottom axis is a transformation of  $\alpha$ .

Here is the best CV tree as plotted by rpart.



#### In R:

```
library(rpart)
library(MASS)
data(Boston)
attach (Boston)
set.seed(99)
#fit a single tree and plot variable importance
#fit a big tree using rpart.control
big.tree = rpart(medv~.,method="anova",data=Boston,
                        control=rpart.control(minsplit=5,cp=.0005))
nbig = length(unique(big.tree$where))
cat("size of big tree: ",nbig,"\n")
#look at CV results
plotcp(big.tree)
iibest = which.min(big.tree$cptable[,"xerror"]) #which has the lowest error
bestcp=big.tree$cptable[iibest,"CP"]
bestsize = big.tree$cptable[iibest,"nsplit"]+1
#prune to good tree
best.tree = prune(big.tree,cp=bestcp)
```

# 6. Bagging and Random Forests

A key idea in modern statistics is the bootstrap:

Treat the sample as if it were the population and then take iid draws.

That is, you sample with replacement so that you can get the same original sample value more than once in a bootstrap sample.

We can use the bootstrap to make tree *much* better predictors !!!!

## To Bootsrap Aggregate (Bag) we:

- ► Take *B* bootstrap samples from the training data, each of the same size as the training data.
- ► Fit a *large* tree to each bootstrap sample (we know how to do this fast!). This will give us B trees.
- ► Combine the results from each of the *B* trees to get an overall prediction.

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For numeric y we can combine the results easily by making our overall prediction the average of the predictions from each of the B trees.

For categorical *y*, it is not quite so obvious how you want to combine the results from the different trees.

Often people let the trees vote: given x get a prediction from each tree and the category that gets the most votes (out of B ballots) is the prediction.

Alternatively, you could average the  $\hat{p}$  from each tree. Most software seems to follow the vote plan.

## Why on earth would this work??!!

Remember our basic intuition about averaging, for

$$y_i = \mu + \epsilon_i$$

we think of  $\mu$  as the signal and  $\epsilon_i$  as the noise part of each observation.

When we average the  $y_i$  to get  $\bar{y}$ , the signal,  $\mu$ , is in each draw, so it does not wash away, but the  $\epsilon_i$  wash out.

For us, the *signal* is the part of y we can guess from knowing x!!

Bagging works the same way.

We randomize our data and then build a lot of big (and hence noisy!) trees.

The relationships which are real get captured in a lot of the trees and hence do not wash out when we average.

Stuff that happens "by chance" is idiosyncratic to one (or a few) trees and washes out in the average.

Brilliant. Leo Brieman.

#### Note:

You need B big enough to get the averaging to work, but it does not seem to hurt if you make B bigger than that.

The cost of having very large B is in computational time.

We can build trees fast, but if you start building thousands of really big trees on large data sets, it can end taking a while.

#### Random Forests:

Random Forests starts from Bagging and adds another kind of randomization.

Rather than searching over all the  $x_i$  in x when we do our greedy build of the big trees, we randomly sample a subset of m variables to search over each time we make a split.

This makes the big trees "move around more" so that we explore a rich set of trees, but the important variables will still shine through!!.

### Have to choose:

- B: number of Bootstrap samples (hundreds, thousands).
- ▶ m: number of variables to sample.

A common choice is  $m = \sqrt{p}$ , where p is the dimension of x.

#### Note:

Bagging is Random Forests with m = p.

#### Note:

There is no explicit regularization parameter as in the lasso and single tree prediction.

### OOB Error Estimation:

OOB is "Out of Bag".

For a bootstrap sample, the observations chosen are "in the bag" and the rest are out.

There is a very nice way to estimate the out-of-sample error rate when bagging.

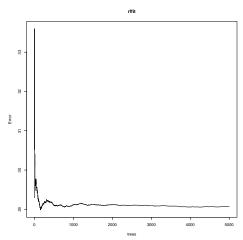
One can show that, on average, each bagged tree makes use of about 2/3 of the observations.

By carefully keeping track of which bagged trees use which observations you can get out-of-sample predictions.

## Bagging for Boston: y=medv, x=lstat.

Here is the error estimation as a function of the number of trees based on OOB.

Suggests you just need a couple of hundred trees.

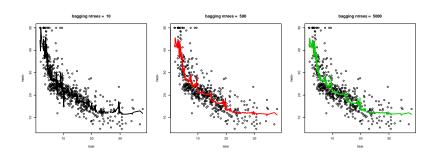


## Bagging for Boston: y=medv, x=lstat.

With 10 trees our fit is too jumbly.

With 1,000 and 5,000 trees the fit is not bad and very similar.

Note that although our method is based on trees, we no longer have a simple step function!!



# 7. Boosting Trees

Like Random Forests, boosting is an *ensemble method* is that the overall fit it produced from many trees.

The idea however, is totally different!!

## In Boosting we:

- Fit the data with a single tree.
- Crush the fit so that it does not work very well.
- Look at the part of y not captured by the crushed tree and fit a new tree to what is "left over".
- Crush the new tree. Your new fit is the sum of the two trees.
- Repeat the above steps iteratively. At each iteration you fit "what is left over" with a tree, crush the tree, and then add the new crushed tree into the fit.
- Your final fit is the sum of many trees.

This one is actually made clearer by the mathematical notation. This is Algorithm 8.2 (page 322) in the book.

## For Numeric *y*:

- (i) Set  $\hat{f}(x) = 0$ .  $r_i = y_i$  for all i in the training set.
- (ii) for b = 1, 2, ... B, repeat:
  - Fit a tree  $\hat{f}^b$  with d splits (d+1) terminal nodes to the training data (X, r).
  - ▶ Update  $\hat{f}$  by adding in a shrunken version of the new tree:  $\hat{f}(x) \leftarrow \hat{f}(x) + \lambda \hat{f}^b(x)$ .
  - ▶ Update the residuls:  $r_i \leftarrow r_i \lambda \hat{f}^b(x)$ .
- (iii) Output the boosted model:

$$\hat{f}(x) = \sum_{i=1}^{B} \lambda \, \hat{f}^b(x).$$

#### Note:

 $\lambda$  is the "crushing" or "shrinkage" parameter.

It make each new tree a *weak learner* in that is only does a little more fitting.

#### Have to choose:

- ▶ B, number of iterations (the number of trees in the sum) (hundreds, thousands).
- d, the size of each new tree.
- λ, the crush factor.

#### Note:

Boosting for categorical *y* works in an analogous manner but it is more messy how you define "the part left over", you can't just use residuals.

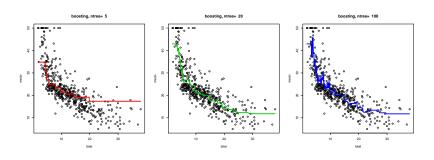
Also you can't just add up the fit.

But, it is the same idea:

- ► fit.
- crush fit.
- fit what is left over.
- aggregate crushed fits.

# Boosting for Boston: y=medv, x=lstat:

Here are some boosting fits where we vary the number of trees, but fix the depth at 2 (suitable with 1 x) and shrinkage  $= \lambda$  at .2.



Again, this ensemble method gets away from the crude step function given by a single tree.

# 8. Variable Importance Measures

The ensemble methods Random Forests and Boosting can give dramatically better fits than simple trees. Out-of-sample, they can work amazingly well. They are a breakthrough in statistical science.

However, they are certainly not interpretable!!

You cannot look at hundreds or thousands of trees.

Nonetheless, by computing summary measures, you can get some sense of how the trees work.

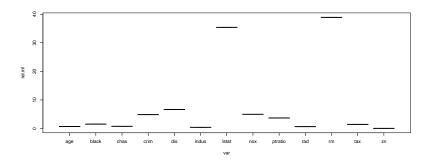
In particular, we are often interested in which variables in  $\boldsymbol{x}$  are really the "important" ones.

What we do is look at the splits (decision rules) in a tree and pick out the ones that use a particular variable. Then we can add up the reduction in loss (eg residual sum of squares) due to the splits using the variable.

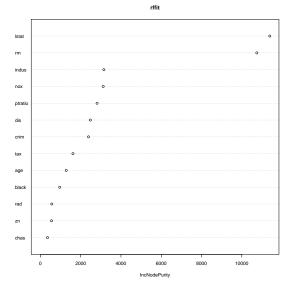
For a single tree we are done.

For bagging we can average the effect of a variable over the B trees and for Boosting we can sum the effects.

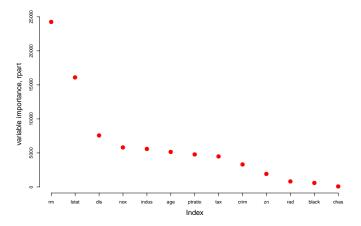
Here is the variable importance for the Boston data with all the variables obtained from a Boosting fit.



Here is the variable importance for the Boston data with all the variables obtained from a Random Forests fit.



Here is the variable importance for the Boston data with all the variables obtained from a single tree fit (using rpart).



9. Trees, Random Forests, Boosting: The California Data

Let's try all this stuff on the California Housing data.

That is, we'll try trees, Random Forests, and Boosting.

How will they do !!!

We'll do a simple three set approach since we have a fairly large data set.

We randomly divide the data into three sets:

Train: 10,320 observations.

**Validation:** 5,160 observations.

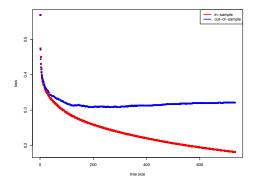
Test: 5,160 observations.

We,

- Try various approaches using the Training data to fit and see how well we do out-of-sample on the Validation data set.
- ► After we pick an approach we like, we fit using the combined Train+Validation and then predict on the test to get a final out-of-sample measure of performance.

### Trees:

- Fit big tree on train.
- For many cp=α, prune tree, giving trees of various sizes.
- Get in-sample loss on train
- Get out-of-sample loss on validation



The loss is RMSE.

We get the smallest out-of-sample loss (.307) at a tree size of 194.

# Boosting:

## Let's try:

- maximum depths of 4 or 10.
- ▶ 1,000 or 5,000 trees.
- ▶  $\lambda = .2 \text{ or } .001.$

		tdepth	ntree	lam	olb	ilb
olb:	1	4	1000	0.001	0.414	0.416
out-of-sample loss	2	10	1000	0.001	0.378	0.380
ilb:	3	4	5000	0.001	0.279	0.282
in-sample loss.	4	10	5000	0.001	0.252	0.250
	5	4	1000	0.200	0.232	0.164
min loss of .231 is quite a bit better than trees!	6	10	1000	0.200	0.233	0.098
	7	4	5000	0.200	0.231	0.081
	8	10	5000	0.200	0.233	0.014

### Random Forests:

## Let's try:

- m equal 3 and 9 (Bagging).
- ▶ 100 or 500 trees.

olrf is the out-of-sample loss and ilrf is the in-sample loss.

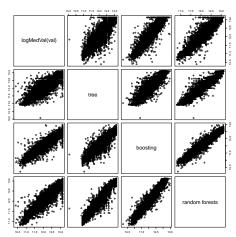
```
mtry ntree olrf ilrf
1 9 100 0.241 0.255
2 3 100 0.236 0.250
3 9 500 0.241 0.253
4 3 500 0.233 0.245
```

Minimum loss is comparable to boosting.

Let's compare the predictions on the Validation data with the best performing of each of the three methods.

It does look like Boosting and Random Forests are a lot better than a single tree.

The fits from Boosting and Random Forests are not too different (this is not always the case).

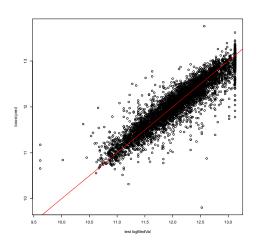


## Test Set Performance, Boosting

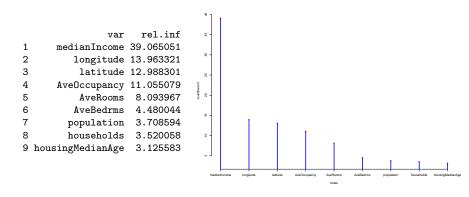
Let's fit Boosting using depth=4, 5,000 trees, and shrinkage =  $\lambda$ =.2 on the combined train and validation data sets.

The RMSE on test data is .231.

This is consistent with what we had before from the trainvalidation data.



Boosting gives us a measure of variable importance:

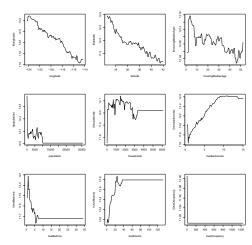


medianIncome is by far the most important variable. After that, it is location - makes sense.

The boosting package also generated plot which are supposed to show the plot of  $x_i$  vs. y for each individual  $x_i$  by averaging out the other x's.

This is supposed to be a plot of  $x_i$  vs.  $y = \log Med Val$  for each i = 1, 2, ..., 9.

It is not clear this works, or should work, when there are interactions!!



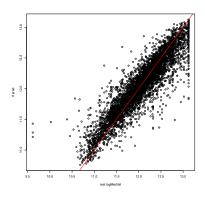
## Test Set Performance, Random Forests

Let's fit Random Forests using m=3 and 500 trees on the combined train and validation data sets.

Let's see how the predictions compare to the test values.

Not too bad!!

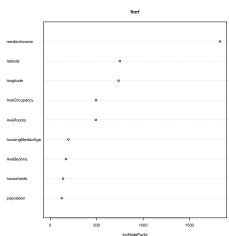
The RMSE is .23, so our train-validation results hold up.



## Random Forests: Variable Importance:

Random Forests give a measure of variable importance. It just adds up how much the loss decreases every time a variable is used in a split.

Not suprisingly, medianIncome is by far the most important variable.



## In R:

```
#load libraries
library(randomForest)
library(gbm) #boosting
#-----
#read in California Housing Data
ca = read.csv("calhouse.csv")
#train, val , test
set.seed(14) #Dave Keon was captain of the Toronto Maple Leafs!!!
n=nrow(ca)
n1=floor(n/2)
n2=floor(n/4)
n3=n-n1-n2
ii = sample(1:n,n)
catrain=ca[ii[1:n1],]
caval = ca[ii[n1+1:n2],]
catest = ca[ii[n1+n2+1:n3],]
```

```
#fit using random forests (on train, predict on val)
#mtry is the number of variables to try
rffit = randomForest(logMedVal~.,data=catrain,mtry=3,ntree=500)
rfvalpred = predict(rffit,newdata=caval)
#fit using boosting
boostfit = gbm(logMedVal~.,data=catrain,distribution="gaussian",
             interaction.depth=4,n.trees=5000,shrinkage=.2)
boostvalpred=predict(boostfit,newdata=caval,n.trees=5000)
#-----
#plot (out-of-sample) fits
pairs(cbind(caval$logMedVal,rfvalpred,boostvalpred))
print(cor(cbind(caval$logMedVal,rfvalpred,boostvalpred)))
```

Let's combine the train and validation data set and refit using boosting.

Then we'll get our out-of-sample rmse from the test data.

```
catrainval = rbind(catrain, caval) #stacks the two data frames
#-----
#refit boosting
boostfit2 = gbm(logMedVal~.,data=catrainval,distribution="gaussian",
           interaction.depth=4,n.trees=5000,shrinkage=.2)
boosttestpred=predict(boostfit2,newdata=catest,n.trees=5000)
#plot test y vs test predictions
plot(catest$logMedVal,boosttestpred)
abline(0,1,col="red",lwd=2)
#-----
rmse = sqrt(mean((catest$logMedVal-boosttestpred)^2))
cat("rmse on test for boosting: ",rmse."\n")
#-----
#variable importance from boosting
summary(boostfit2)
```

Here is code for doing logit, rf, and boosting with a binary categorical y.

We have a training data data frame trainDf and a test df testDf.

```
phatL = list() #store the test phat for the different methods here
###fit logit
lgfit = glm(y~.,trainDf,family=binomial)
print(summary(lgfit))
#predict using logit
phat = predict(lgfit,testDf,type="response")
phatL$logit = matrix(phat,ncol=1) #logit phat
```

```
##settings for randomForest
p=ncol(trainDf)-1
mtryv = c(p, sqrt(p))
ntreev = c(500,1000)
setrf = expand.grid(mtryv,ntreev)
colnames(setrf)=c("mtry","ntree")
phatL$rf = matrix(0.0,nrow(testDf),nrow(setrf))
###fit rf
for(i in 1:nrow(setrf)) {
   cat("on randomForest fit ",i,"\n")
   print(setrf[i,])
   #fit and predict
   frf = randomForest(y~.,data=trainDf,mtry=setrf[i,1],ntree=setrf[i,2])
   phat = predict(frf,newdata=testDf,type="prob")[,2]
  phatL$rf[,i]=phat
```

```
##settings for boosting
idv = c(2,4)
ntv = c(1000.5000)
shv = c(.1..01)
setboost = expand.grid(idv,ntv,shv)
colnames(setboost) = c("tdepth", "ntree", "shrink")
phatL$boost = matrix(0.0,nrow(testDf),nrow(setboost))
trainDfB = trainDf; trainDfB$y = as.numeric(trainDfB$y)-1
testDfB = testDf; testDfB$y = as.numeric(testDfB$y)-1
##fit boosting
for(i in 1:nrow(setboost)) {
   cat("on boosting fit ",i,"\n")
   print(setboost[i,])
   ##fit and predict
   fboost = gbm(y~.,data=trainDfB,distribution="bernoulli",
              n.trees=setboost[i,2],interaction.depth=setboost[i,1],
                         shrinkage=setboost[i,3])
   phat = predict(fboost,newdata=testDfB,n.trees=setboost[i,2],type="response")
   phatL$boost[,i] = phat
```